

# ECO 442: Quantitative Trade Models

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# Trade Costs and Tariffs

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So far in our models, international trade has been frictionless

- Instantly teleport goods from one country to another at no cost
- Obviously not true! Prices are not equal everywhere.

Focus on two primary trade costs

- **Iceberg Trade Costs**
- **Tariffs**

# Iceberg Trade Costs

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**Iceberg Trade Costs** are costs associated with transporting goods across countries

- Fuel to ship the goods
- Loss of product due to spoilage
- Additional workers needed to fill out paper work and follow international regulations

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Iceberg trade costs means to deliver 1 unit of exports, necessary to ship  $\tau > 1$  units

- Effectively the same as lowering productivity for goods sent abroad
- For simplicity, we set domestic iceberg trade costs as  $\tau = 1$

# Tariffs

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**Tariffs** are a tax imposed on imports ([See Tariffs in PE Framework](#))

- Tariffs are redistributed to consumers in the country imposing the tariff

$$\text{Income} = \overbrace{wL}^{\text{Labor Income}} + \overbrace{T}^{\text{Tariff Income}}$$

- Unlike iceberg costs, physical output is not directly affected
- Like iceberg costs, the presence of Tariffs changes equilibrium allocations vs a frictionless world
- Tariffs are typically ad-valorem (applied proportionally to value). Model as

price with tariff = tariff  $\times$  price without tariff

$$p^{\text{import}} = \tau p^{\text{world}}$$

# Multi-Good Ricardian Model of Trade

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Comparative advantage: countries differ in technology and therefore opportunity costs.

- 2x2 Ricardian Model is simple. Tariffs too high  $\Rightarrow$  stop trading.
- Tariffs more interesting with multiple goods (adds middleground between Trade and Autarky)
- We can extend our framework to a large number of goods in a straightforward way

# Model Setup

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- Two countries, indexed by  $i, j = H, F$
- $M$  goods, indexed by  $m$
- Labor ( $L^i$ ) is only factor of production, supplied inelastically
- Countries differ in labor productivities for each good:
  - Productivity in country  $i$  for producing good  $m$  is:  $z_{m,i}$

# Tariff Trade Costs

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Tariffs go on prices rather than in production function

- Let  $p_{m,i}^j$  be the price firms producing good  $m$  in country  $i$  charge to consumers in country  $j$ , then consumers in country  $j$  actually pay

$$\text{Price with Tariff} = \text{Tariff Rate} * \text{Price} = \tau_{m,i}^j p_{m,i}^i$$

- Where  $\tau_{m,i}^j$  is the tariff country  $j$  charges on imports of good  $m$  originating from country  $i$
- What this means, is that the price for consumers in the importing country is  $\tau_{m,i}^i$  times higher than the price the exporting firm's receive for the good



# Tariff Revenue

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Tariff Revenue is generated by the importing country and redistributed to consumers in that country.

Let  $j$  be the importing country and suppose country  $i$  is the other country, then

$$T^j = \sum_{m=1}^M (\tau_{m,i}^j - 1) p_{m,i}^j c_{m,i}^j; \quad i \neq j$$

- Where  $c_{m,i}^j$  is how many units of good  $m$ , consumers in country  $j$  consume that is produced in country  $i$ .

# Equilibrium Definition With Tariffs

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Equilibrium Definition Summary ([Click for Full Definition](#))

- Wages:  $w^H, w^F$ ; Prices for each good for each country:  $p_{m,i}^j, m = 1, \dots, M; i = H, F$
- Consumption, labor input, and production for each good:  $c_{m,i}^j, y_{m,i}^j, l_{m,i}^j, m = 1, \dots, M; i, j = H, F$
- **Tariff Revenue:  $T^j, j = H, F$ . Such that**
  - 1) Given prices and wages, consumers maximize utility subject to budget constraint
  - 2) Firms maximize profit for each good, origin, and destination
  - 3) Markets clear (consumption = output, labor used in production sums to labor endowment)
  - 4) Government B.C. Holds: **Tariff Revenue Distributed = Tariff Revenue Collected**

## Example

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Let's consider the example from Dornbusch, Fischer, and Samuelson (1979) [[Click for more Details](#)]

- Suppose  $M$  is very large, so we almost have an infinite number of goods. Say  $M = 10^6$
- Let both countries be the same size, and let the tariff rate be symmetric

$$L_H = L_F = L$$

$$\tau_{m,i}^j = \tau, \quad \text{if } i \neq j \text{ (Note } \tau_{m,i}^i = 1)$$

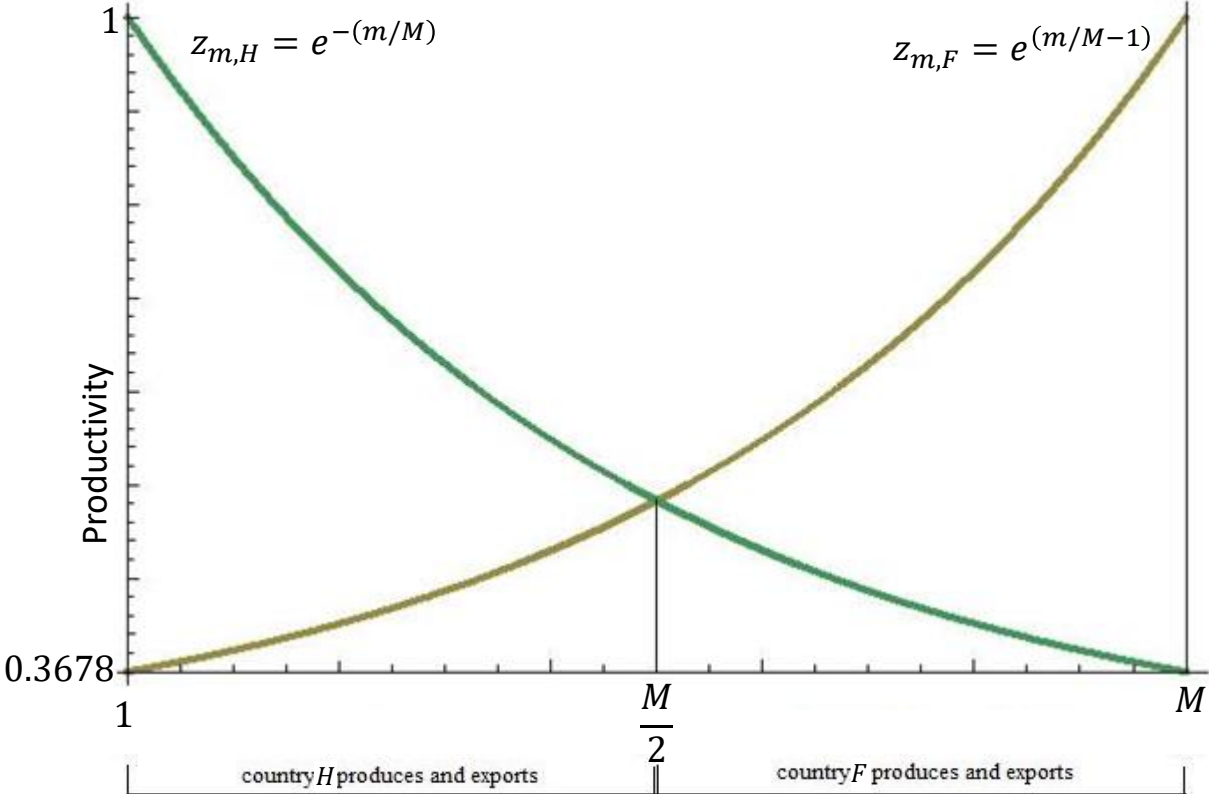
- Suppose the productivity for each good is given by:

$$z_{m,H} = e^{-(m/M)}$$

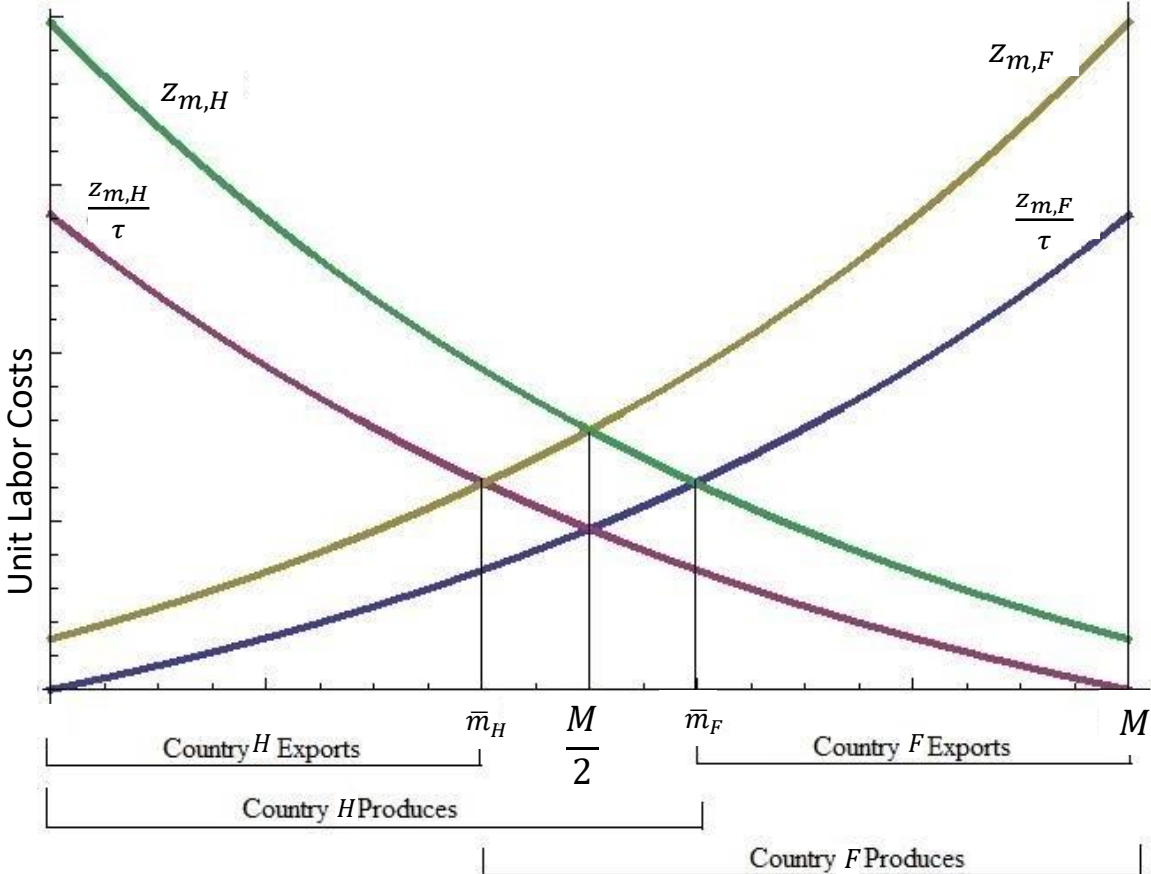
$$z_{m,F} = e^{(m/M-1)}$$

$$\text{E.g. } z_{1,H} = e^{-\frac{1}{10^6}} \approx 0.9999999, \quad z_{1,F} = e^{\frac{1}{10^6}-1} \approx 0.3678, \quad z_{M,H} = e^{-1} \approx 0.3678$$

# Symmetric Equilibrium with Free Trade



# Symmetric Equilibrium: Tariff Trade Costs



# Summary of DFS

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Dornbusch, Fischer, and Samuelson (1979):

- Ricardian model: 2 countries, 1 factor of production, continuum of goods

Strengths:

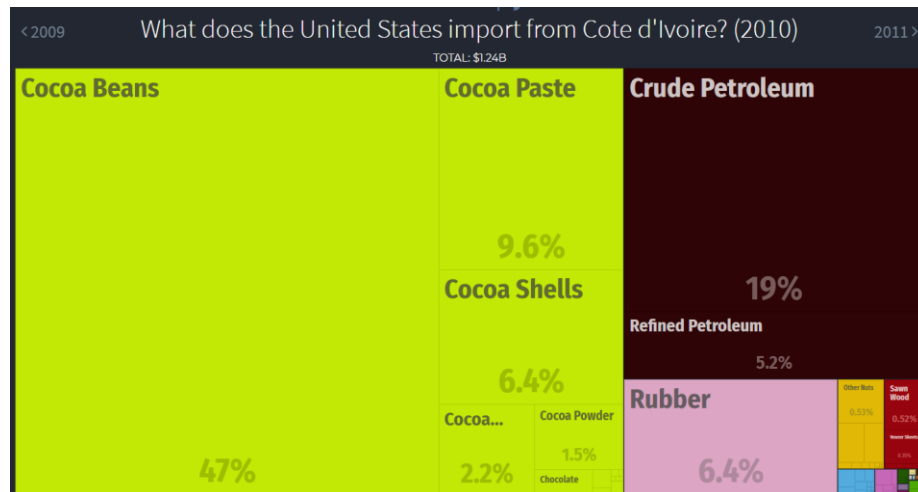
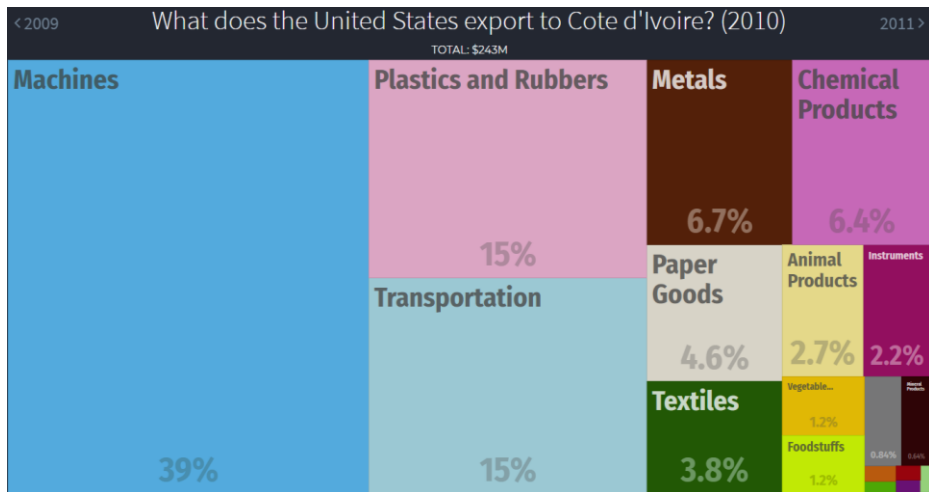
- Simple and intuitive. Can be used to think about effects of trade policy and trade costs.

Weaknesses:

- No explanation for why countries differ in productivity for producing goods
- Not straightforward to extend model to multiple countries

# Is Trade Specialized Like a Ricardian Model Would Predict?

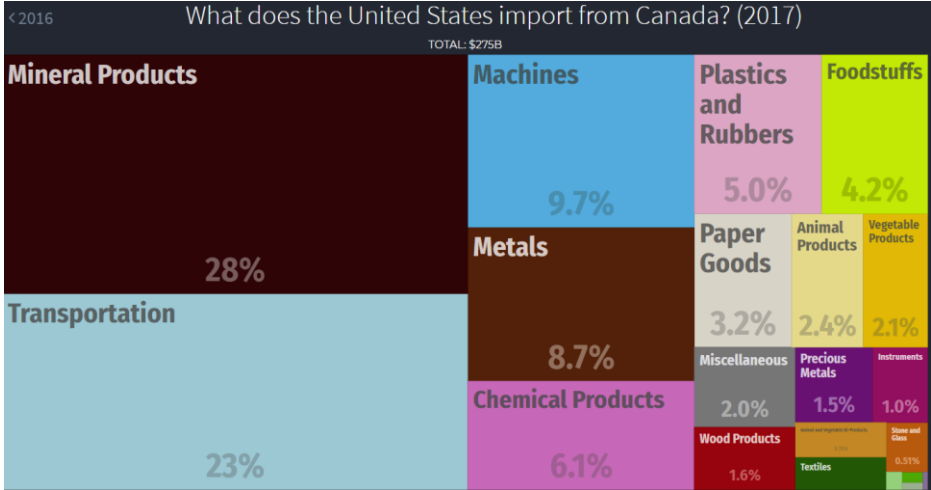
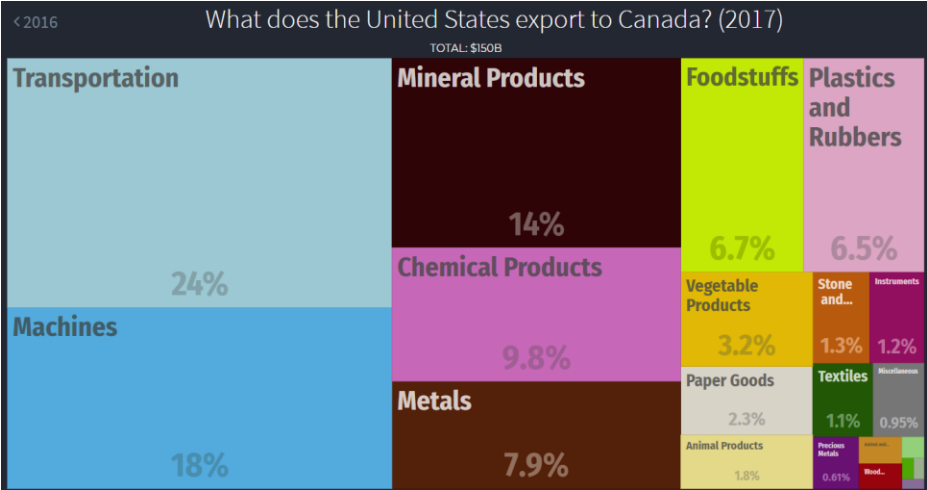
For many developing or commodity rich countries: Yes



US Trade with the Ivory Coast ([From OEC](#))

# Is Trade Specialized Like a Ricardian Model Would Predict?

For Developed Countries: Often Not!

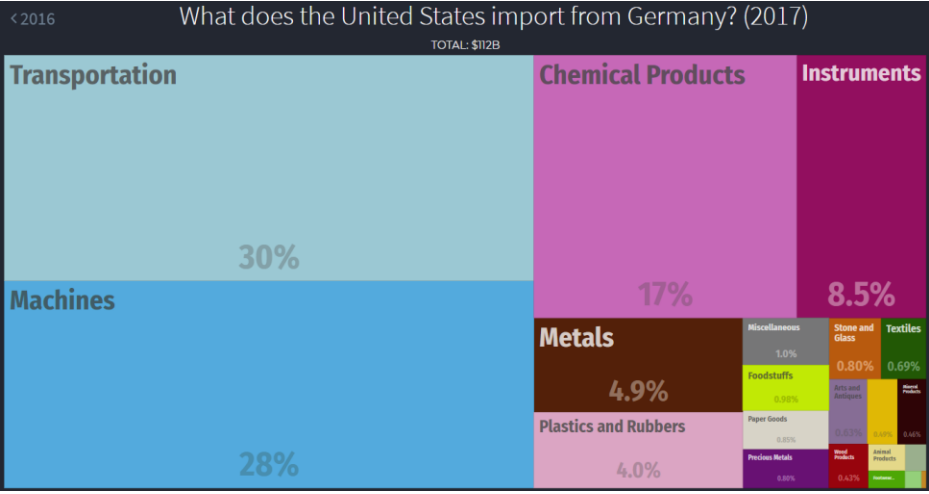
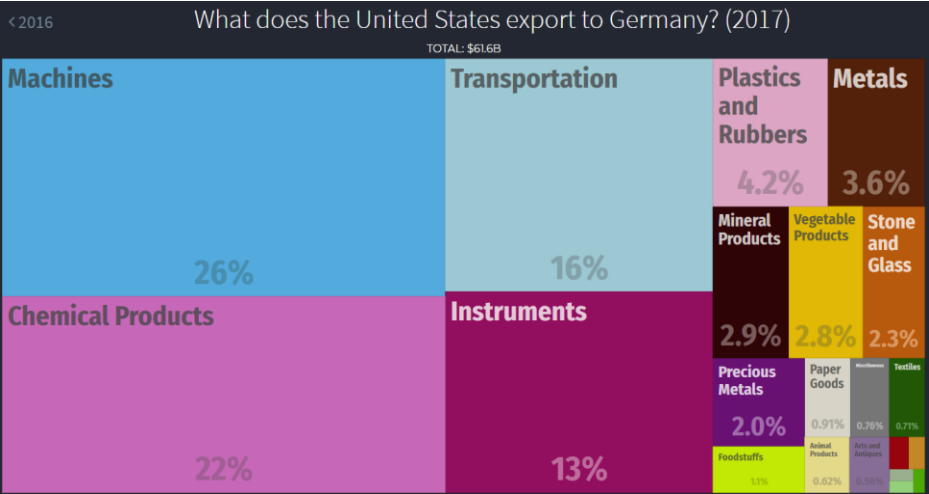


US Trade with Canada ([From OEC](#))



# Is Trade Specialized Like a Ricardian Model Would Predict?

For Developed Countries: Often Not!



US Trade with Germany ([From OEC](#))

Following Slides list the Equilibrium Definition  
and more Details of the Example Set-up

# 1. Consumers problem

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Assume Cobb-Douglas Preferences. Given  $p_{m,i}^j, w^j$  consumer in country  $j$  solve

$$\max \sum_{m=1}^M U(c_{m,H}^j + c_{m,F}^j) = \sum_{m=1}^M \theta_m \log(c_{m,H}^j + c_{m,F}^j)$$

subject to budget constraint ( $T^i$  is transfer from tariffs, zero if no tariffs)

$$\sum_{i=H,F} \sum_{m=1}^M \tau_{m,i}^j p_{m,i}^j c_{m,i}^j = w^j L^j + T^j$$

Non-Negativity:  $c_{m,i}^j \geq 0, m = 1, \dots, M, i = H, F$

Since both goods are inside the log( ), it implies consumers don't care about country of origin

## 2. Firms Problem

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Since we have constant returns to scale, we can separate firm's problem by destination.

Given  $p_{m,i}^j$ ,  $w^i$  firms in country  $i$  maximize profits for good  $m$  for destination  $j$

$$\max p_{m,i}^j y_{m,i}^j - w^i l_{m,i}^j$$

subject to production technology:

$$y_{m,i}^j = z_{m,i} l_{m,i}^j$$

Note: No Tariffs! Also, Productivity doesn't depend on destination!

**Firm Optimization Yields:**  $p_{m,i}^j = \frac{w^i}{z_{m,i}}$  if  $y_{m,i}^j > 0$

### 3. Market Clearing and 4. Gov Budget Constraint

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Goods market clears for each good. We'll just separate it by origin and destination.

$$c_{m,i}^j = y_{m,i}^j, \quad m = 1, \dots, M; i, j = H, F$$

Labor market clears for each country

$$\sum_{j=H,F} \sum_{m=1}^M l_{m,i}^j = L_i, \quad i = H, F$$

#### 4. Government Budget Constraint

$$T^j = \sum_{m=1}^M (\tau_{m,i}^j - 1) p_{m,i}^j c_{m,i}^j; \quad i \neq j$$

# Ordering Goods and Equilibrium Cutoff

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Order each good by decreasing comparative advantage for country  $H$ :

$$\frac{z_1^H}{z_1^F} > \frac{z_2^H}{z_2^F} > \dots > \frac{z_M^H}{z_M^F}$$

- In equilibrium, there will be a good  $\bar{m}$  such that  $H$  produces all goods  $m = 1, 2, \dots, \bar{m}$  and  $F$  produces all goods  $m = \bar{m} + 1, \dots, M$ .
  - This is something you can prove as a theorem, but for our purposes, we can rely on guessing that this is true, finding the cutoff good, and then verifying it's an equilibrium

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- Let both countries be the same size, and let the tariff rate be symmetric

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- Suppose the productivity for each good is given by:

$$z_{m,H} = e^{-(m/M)}$$

$$z_{m,F} = e^{(m/M-1)}$$

$$\text{E.g. } z_{1,H} = e^{-\frac{1}{10^6}} \approx 0.9999999, \quad z_{1,F} = e^{\frac{1}{10^6}-1} \approx 0.3678, \quad z_{M,H} = e^{-1} \approx 0.3678$$

## Symmetric Equilibrium with Free Trade

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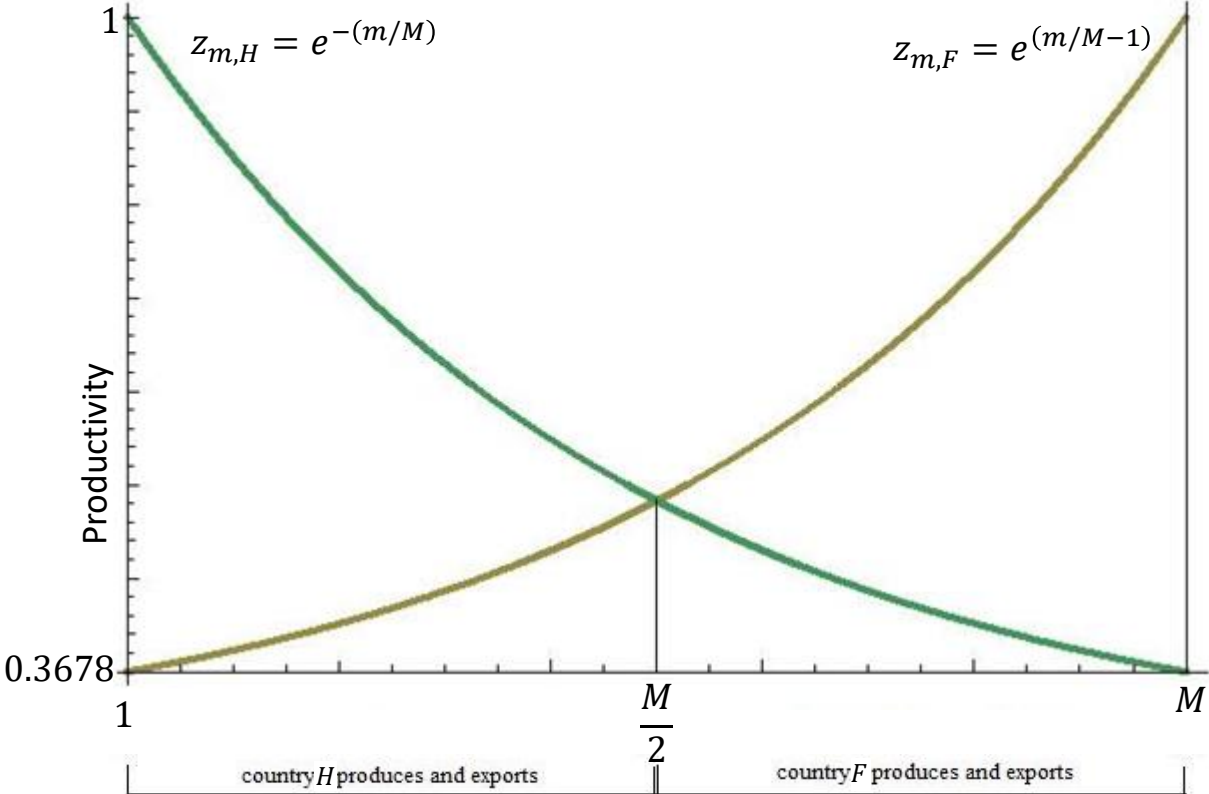
Will have equilibrium with  $w^H = w^F$  (relative wages  $\frac{w^H}{w^F} = 1$ )

Will have cutoff good  $\bar{m} = \frac{M}{2}$

- Country 1 produces and exports goods in  $m = 1, \dots, \bar{m}$
- Country 2 produces and exports goods in  $m = \bar{m} + 1, \bar{m} + 2, \dots, M$



# Graph of Productivities



## Tariff Trade Costs: Cutoffs

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Will no longer have single cutoff

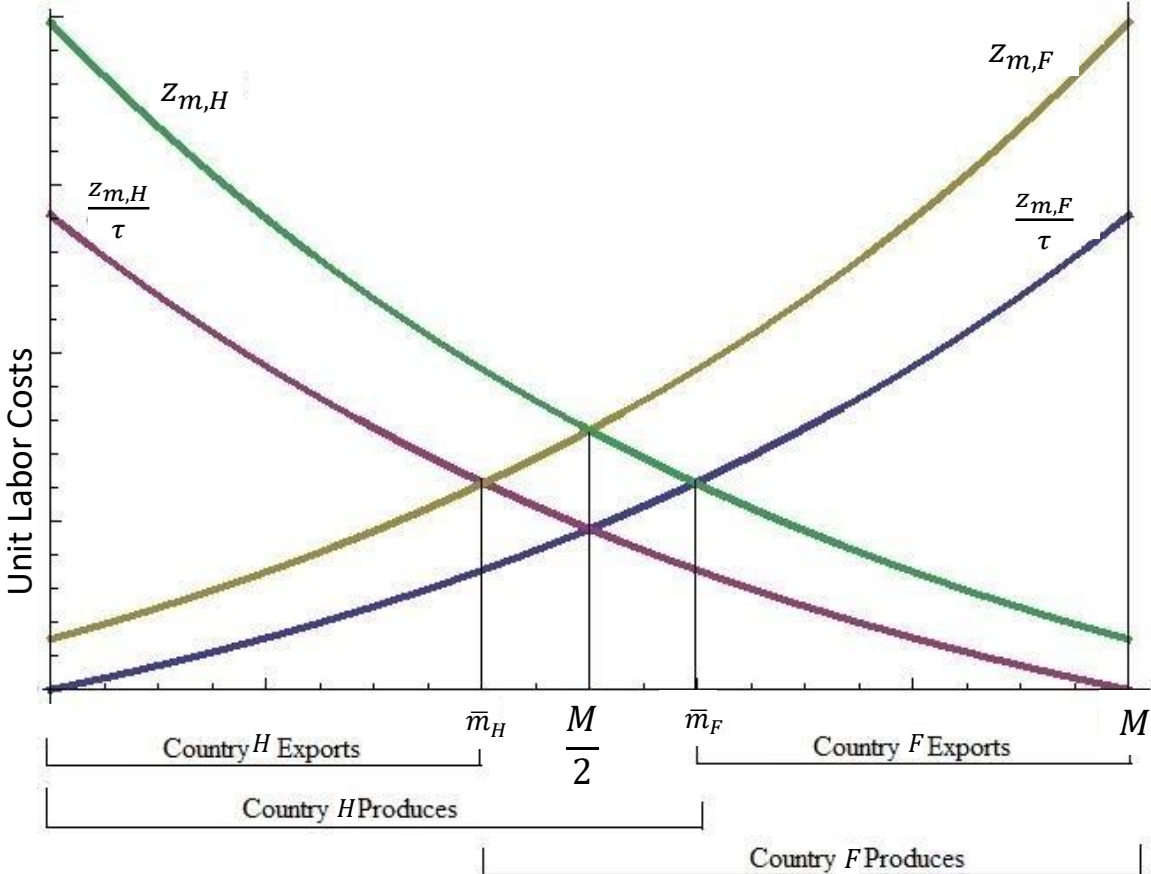
- If  $\tau > \max\left\{\frac{z_{m,H}}{z_{m,F}}, \frac{z_{m,F}}{z_{m,H}}\right\}$  then good will not be exported by either country

Two cutoffs  $\bar{m}_H$  and  $\bar{m}_F$  ( $\bar{m}_F > \bar{m}_H$ ):

- Country 1 produces goods  $m = 1, \dots, \bar{m}_F$ , exports goods  $m = 1, \dots, \bar{m}_H$
- Country 2 produces goods  $m = \bar{m}_H, \dots, M$ , exports goods  $m = \bar{m}_F, \dots, M$

Keep the same symmetric setup, so still have an equilibrium with  $w^H = w^F = 1$ .

# Symmetric Equilibrium: Tariff Trade Costs



## Iceberg Trade Costs:

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Suppose each country faces an iceberg transportation cost of  $\tau > 1$  when exporting:

$$y_{m,i}^j = \frac{l_{m,i}^j}{\tau z_{m,i}}, \quad \text{if } i \neq j$$

Still costless to produce for domestic market:  $y_{m,i}^i = \frac{l_{m,i}^i}{z_{m,i}}$

## Comparison Tariff Trade Costs

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For both iceberg trade costs and tariffs, will have

$$p_{m,i}^j y_{m,i}^j = \begin{cases} \frac{w^i l_{m,i}^j}{\tau}, & \text{if } i \neq j \\ w^i l_{m,i}^j, & \text{if } i = j \end{cases}$$

This means it doesn't matter if we put  $\tau$  on prices or output. Solution to problem is same.

Difference is that tariffs are rebated back to consumers. Consumer budget constraint:

$$\text{Tariffs: } \sum_{i=H,F} \sum_{m=1}^M \tau_{m,i}^j p_{m,i}^j c_{m,i}^j = w^j L^j + T^j$$

$$\text{Iceberg: } \sum_{i=H,F} \sum_{m=1}^M p_{m,i}^j c_{m,i}^j = w^j L^j$$

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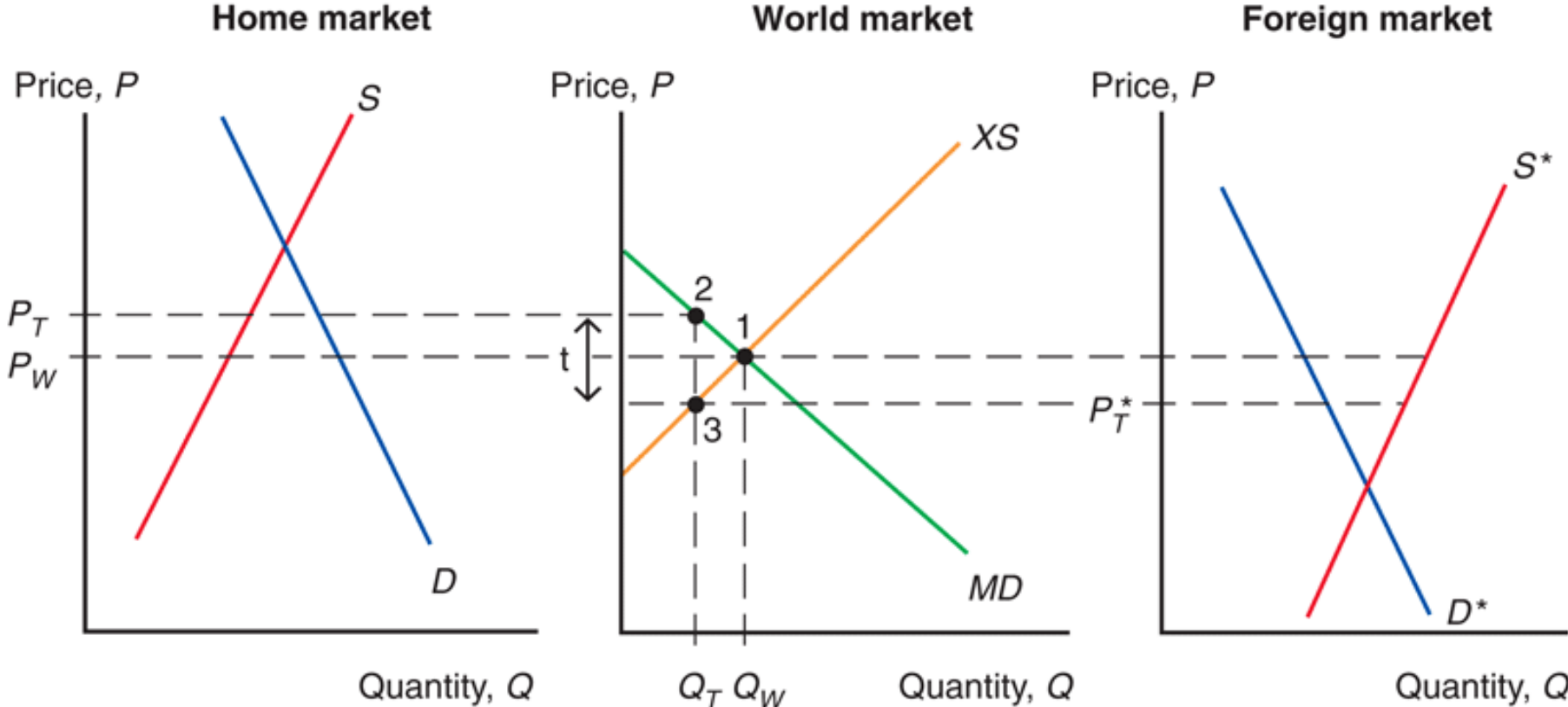
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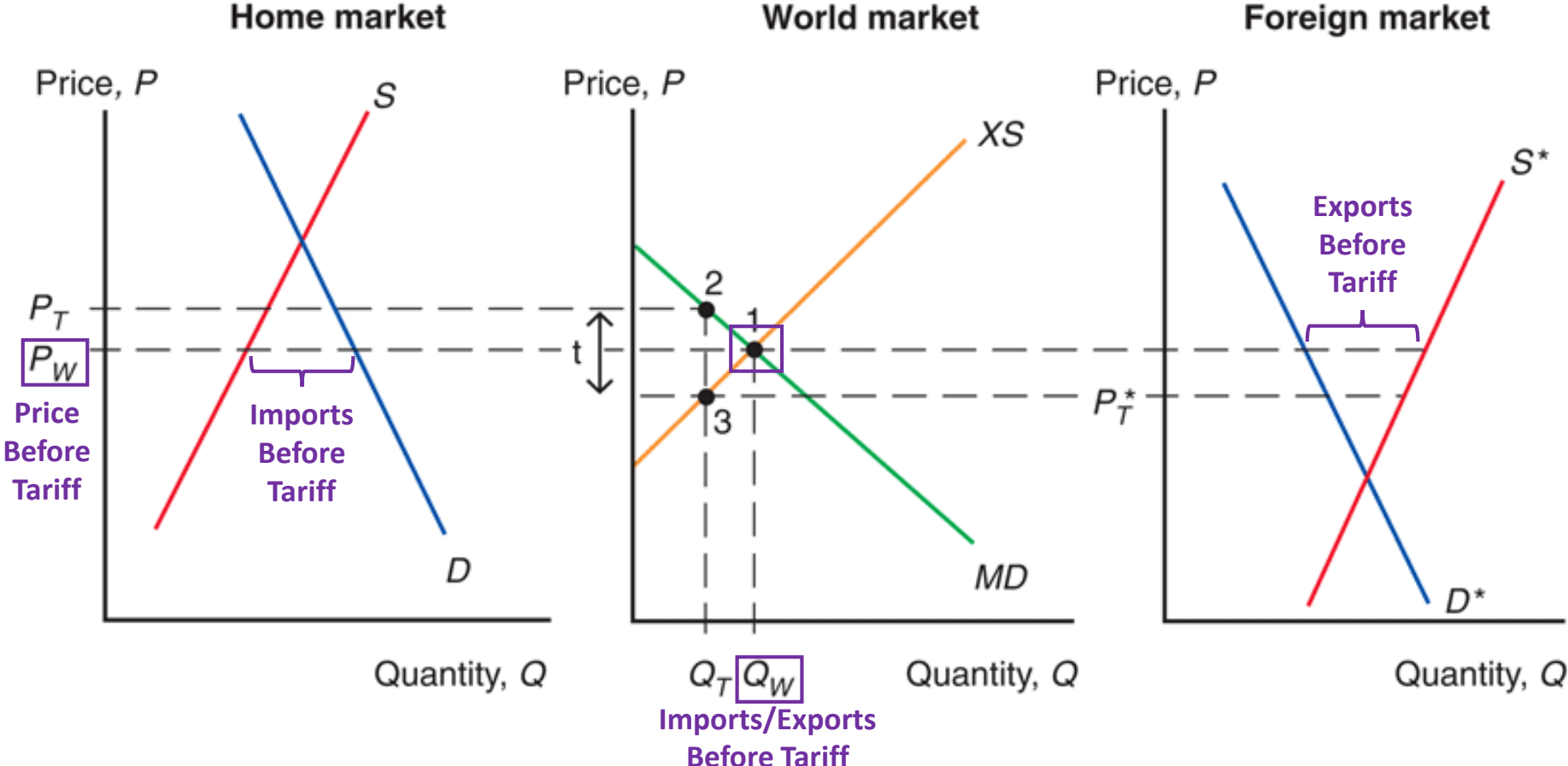
Following Slides briefly show Tariffs in PE Setup

# Effects of an Import Tariff





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